

# Exam 1

Student Name: \_\_\_\_\_

Student ID#: \_\_\_\_\_

Each problem is worth 5 points. Give a complete solution to receive the full credit!

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1. Replace the question mark by  $<$ ,  $>$ , or  $=$ , whichever is correct.

(a)  $\left(\frac{1}{2}\right)^{-2013} ? 2^{2013}$

(b)  $\frac{1}{3} ? 0.3333333333$

(c)  $\sqrt[6]{2} ? \sqrt[3]{\frac{\sqrt{18}}{3}}$

(d)  $e^{-2} ? \frac{1}{e^{-2}}$

(e)  $\sqrt{2} ? 1.4142136$

2. Find the real values  $z$  for which function  $f(z) = \frac{\sqrt{3}}{z-7}$  is defined.

3. Suppose that  $f(x) = 3x + 1$ . Simplify the expression  $\frac{f(x+h)-f(x)}{h}$  where  $h \neq 0$ .

4. Simplify expression:

$$\sqrt[3]{\frac{(yz)^{-3}}{yz\sqrt[7]{y}}}.$$

Express the answer so that all exponents are positive.

5. Find the remainder when  $1 + x^3 - \frac{2}{3}x$  is divided by  $\frac{2}{5}x + 1$ .

6. Factor the polynomial  $P_3(x) = x^3 + x - 2$ . Hint: You might want to try grouping.

7. Perform the indicated operations and simplify. Leave your answer in factored form.

$$\frac{x+2}{x^2-1} - \frac{x+1}{x^2+x-2}$$

8. How many real solutions does the equation  $x^2 - \pi x + 2013 = 0$  have?

9. Evaluate  $\frac{1}{(3-i)^2}$ .

10. Find the zeros of the logistic map  $f(x) = 4x(1-x)$ .